

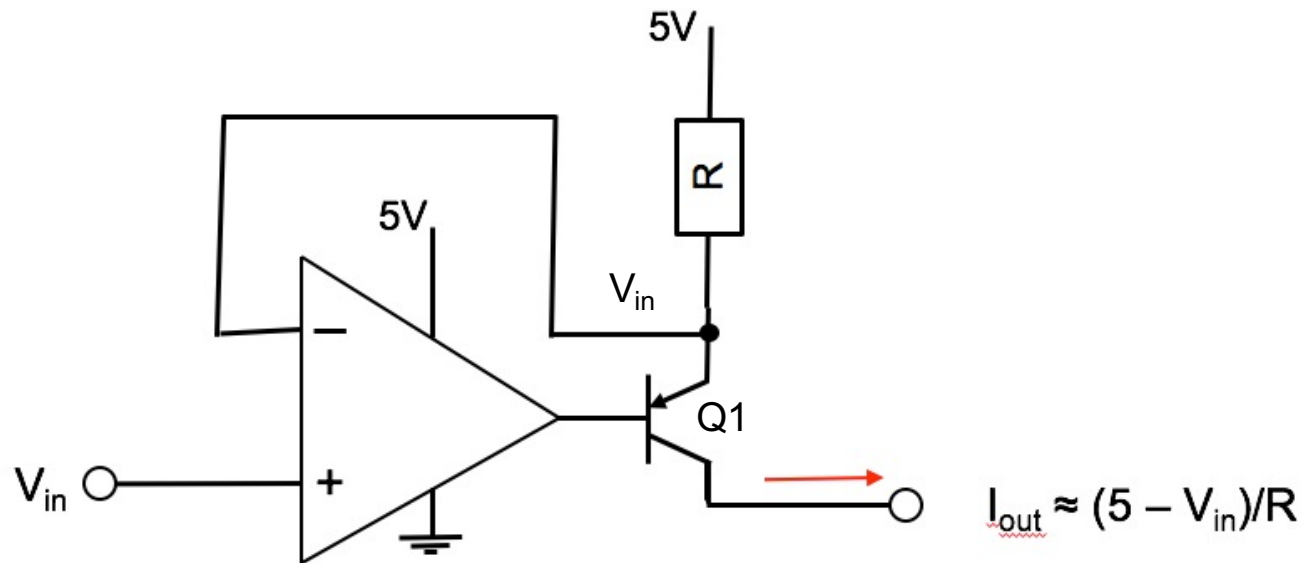
Lecture 4

Applications of Operational Amplifiers

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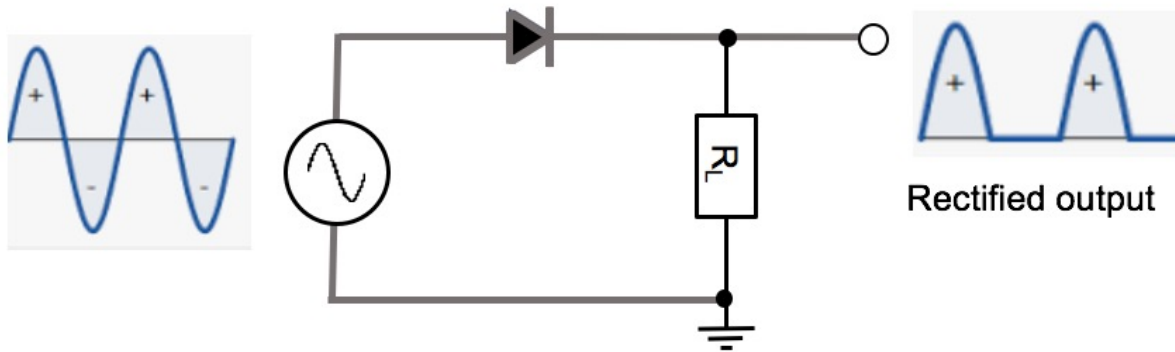
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Voltage to current converter

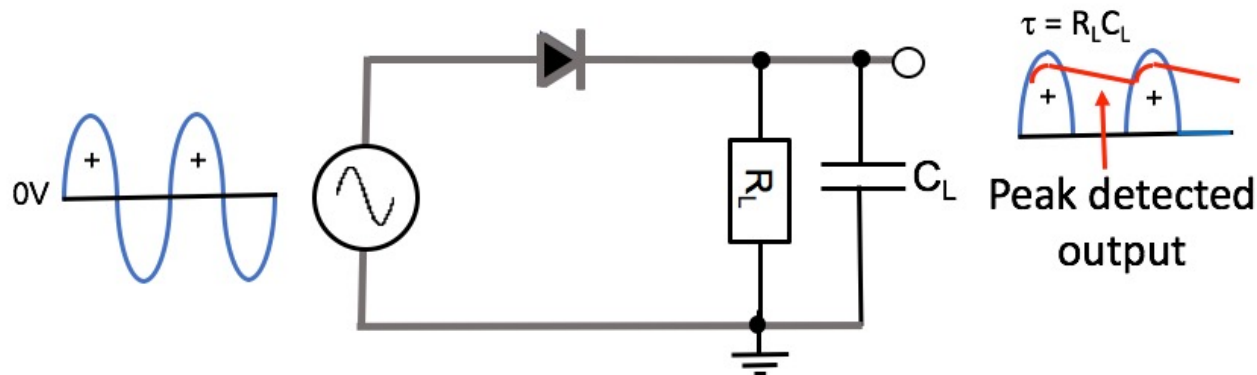


- ❖ PNP transistor $Q1$ must be in linear region
- ❖ Op-amp forces $V_- = V_{in}$
- ❖ R (with 5V) determines the current as $I_R = (5 - V_{in})/R$
- ❖ Assume no current flows into input of op-amp
- ❖ $I_C = I_E - I_B$, assume current gain $\beta \gg 1$, $I_C \approx I_E \approx I_R$
- ❖ Can use FET or MOSFET in place of BJT

Half-wave rectifier & Peak detector

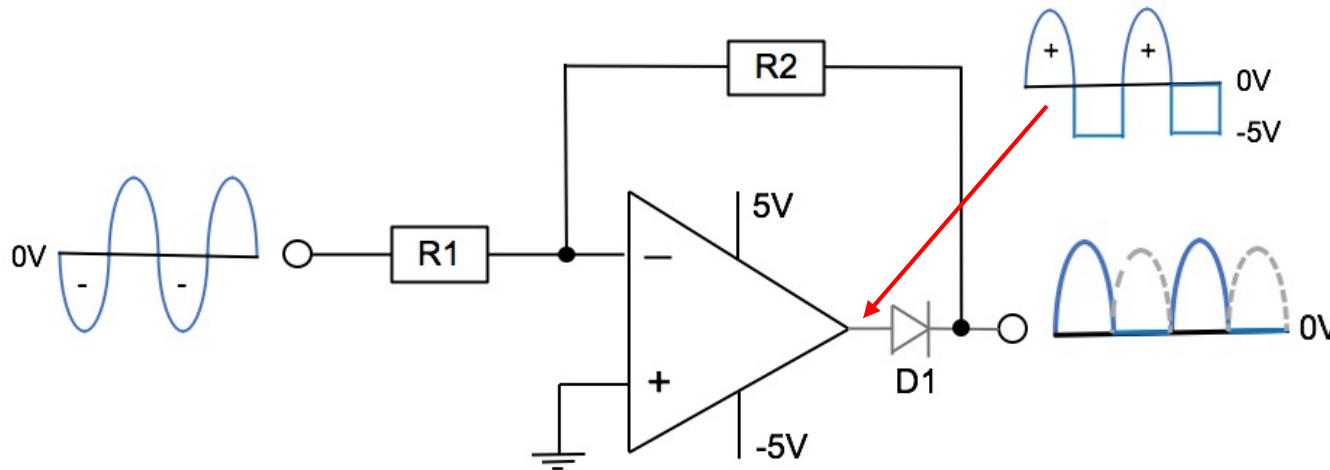


- ❖ Diode and resistor – simple half-wave rectifier
- ❖ Commonly used in power electronics or and multimeters

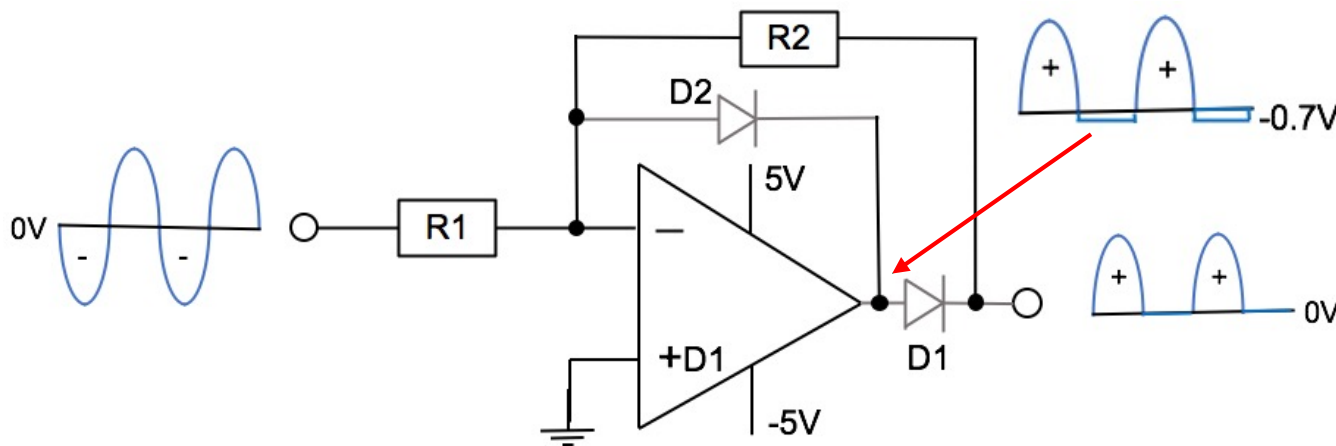


- ❖ C_L charges to V_{in} peak $- V_D$
- ❖ Diode prevents C_L discharging when V_{in} drops
- ❖ R_L discharges capacitor with time constant $R_L C_L$
- ❖ C_L charges again on the positive cycle

Rectifier with op-amp buffering

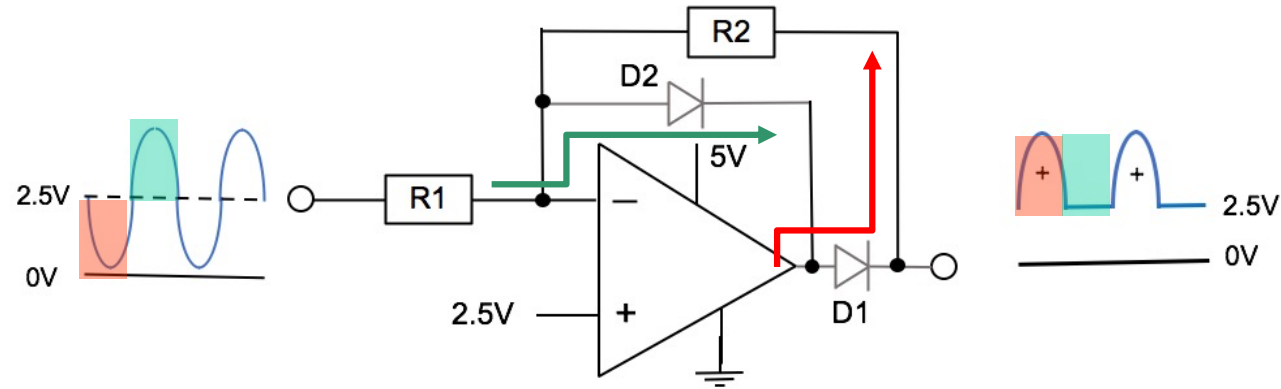


- ❖ Assume $R1 = R2$
- ❖ Negative cycles result in an inverting amplifier with gain = -1
- ❖ Op-amp drives output with low impedance
- ❖ Positive cycles, op-amp isolated from output
- ❖ Poor full-wave rectification



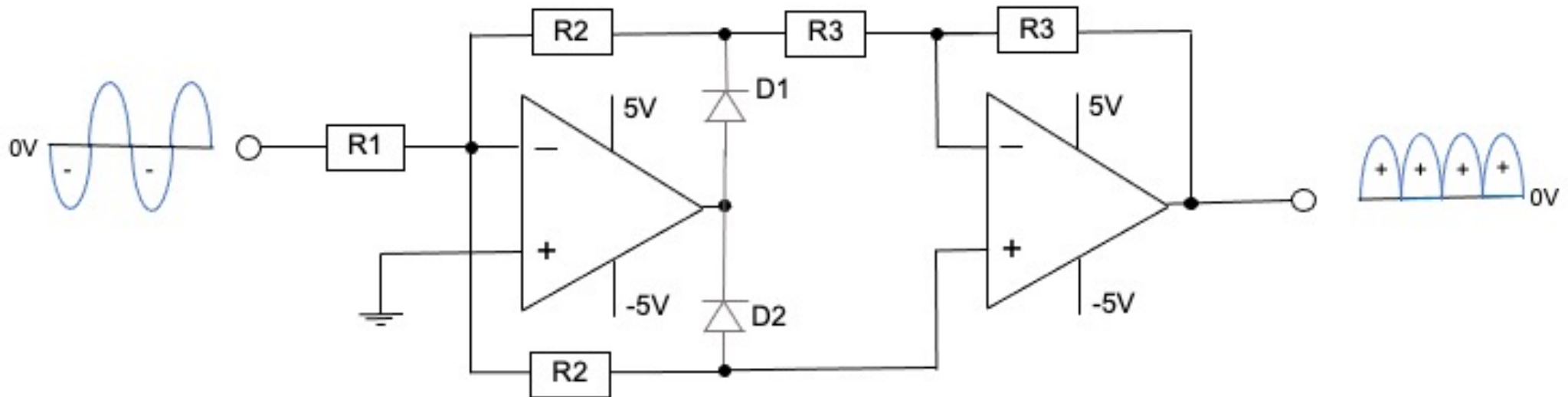
- ❖ D1 provides feedback path for negative input cycles
- ❖ D2 provides feedback path for positive input cycles
- ❖ Op-amp operating throughout entire cycle

Single power supply “rectifier”



- ❖ Single power supply rectifier is implemented by shifting the reference voltage to $\frac{1}{2} V_{DD}$

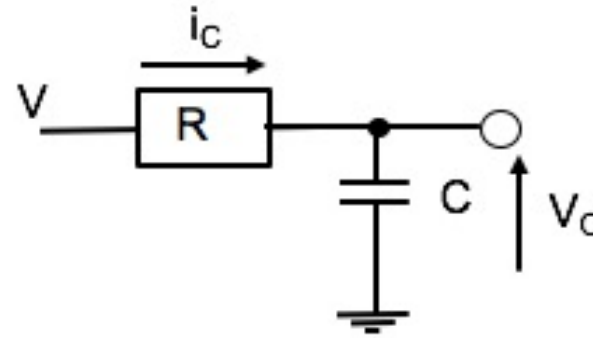
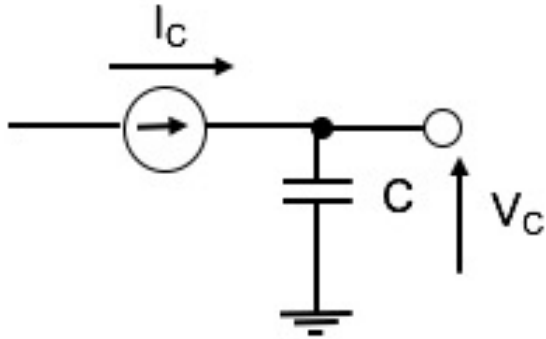
Full-wave rectifier



- ❖ Precision full-wave rectifier with two op-amps
- ❖ Op-amp 1 provides two separate half of the rectified signals
- ❖ Op-amp 2 sums two half cycles together

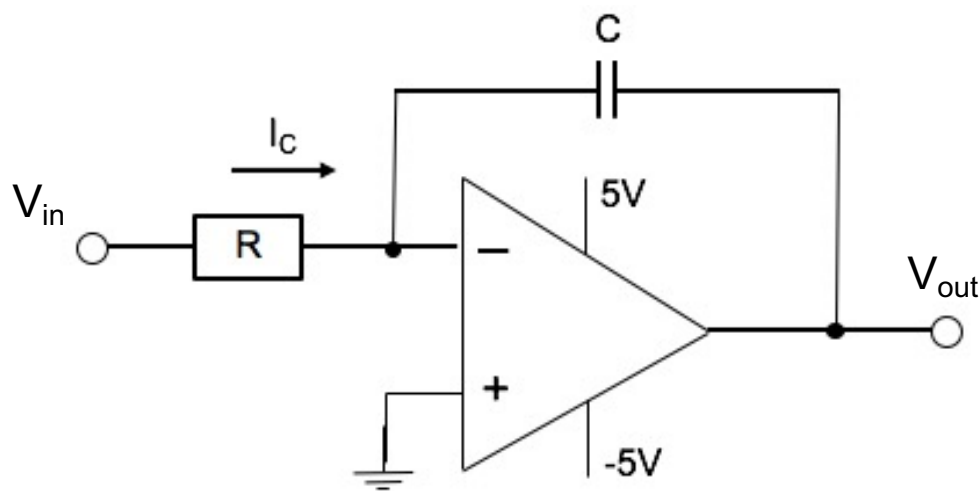
Integrator

$$\diamond i_C = C \frac{dV_C}{dt} \Rightarrow V_C = \frac{1}{C} \int i_C dt + V_C(0)$$

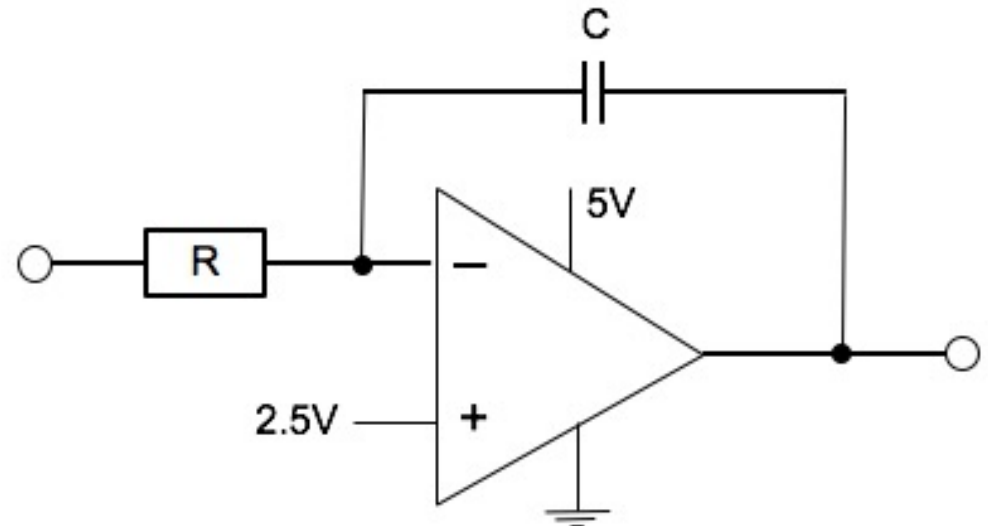


- ❖ I_C changes with V_C
- ❖ V_C is an exponential rise function (not perfect integral)

$$\diamond \text{Constant } I_C, V_C = \frac{i_C}{C} t + V_C(0)$$

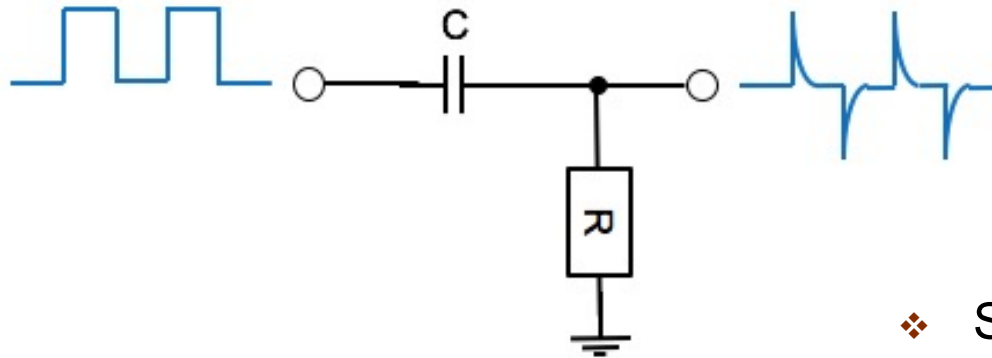


$$\diamond v_{out} = -\frac{V_{in}}{RC} t + V_C(0)$$

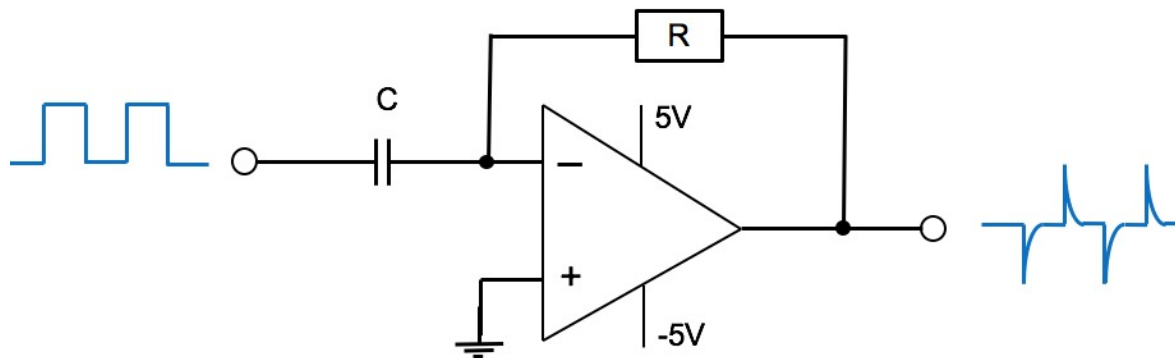


- ❖ Single supply operation

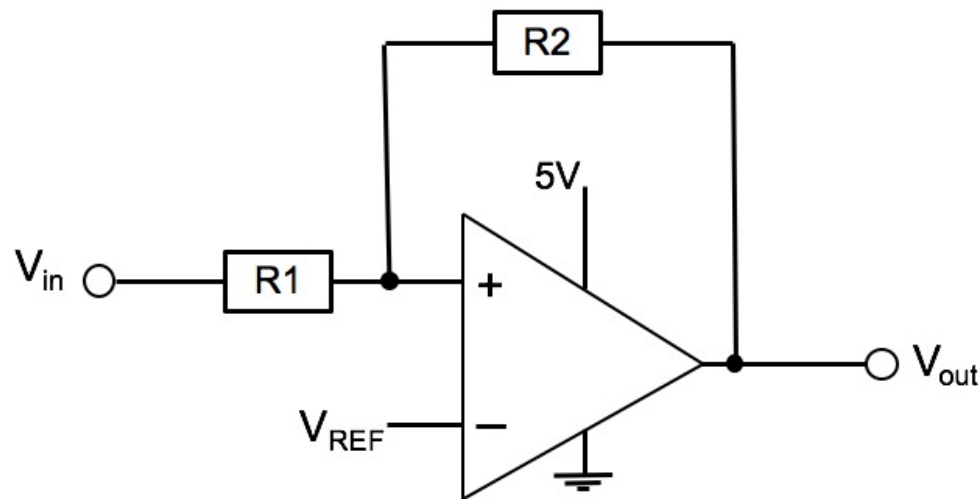
Differentiator



- ❖ Swap R and C
- ❖ Implement a differentiator
- ❖ Not used often because circuit tends to produce noisy output



Comparator with hysteresis



- ❖ V_{out} swings between V_{DD} and V_{SS}
- ❖ V_{out} changes state when V_+ reaches V_{REF}
- ❖ Apply KCL at V_+ :

$$\frac{V_{REF} - V_{in}}{R1} = \frac{V_{out} - V_{REF}}{R2}$$

$$\Rightarrow V_{in} = V_{REF} \left(1 + \frac{R1}{R2} \right) - V_{out} \left(\frac{R1}{R2} \right)$$

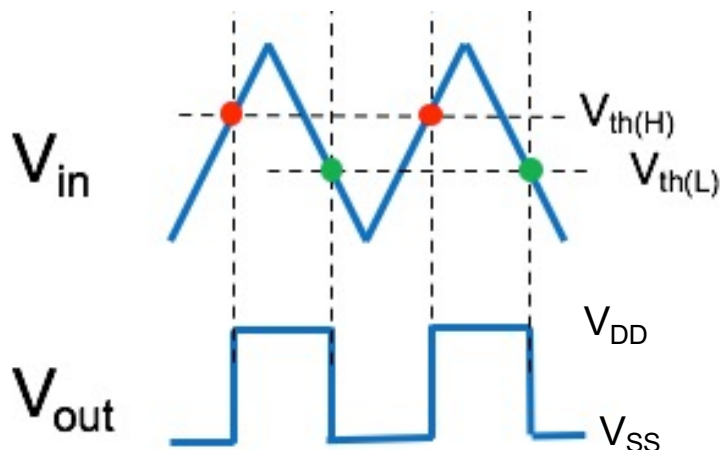
- ❖ If $R1 = 0$ or $R2 = \infty$, $V_{th} = V_{REF}$

- ❖ $R1 > 0, R2 \neq \infty$

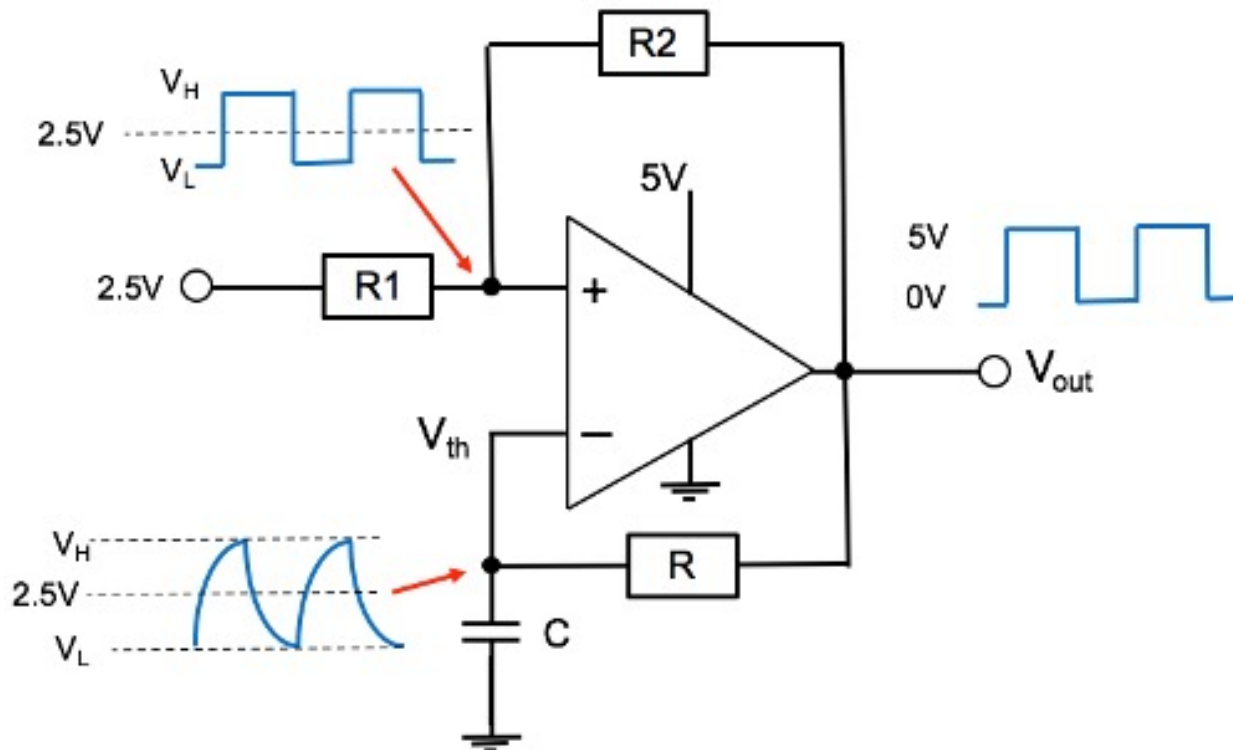
$$V_{th(H)} = V_{REF} \left(1 + \frac{R1}{R2} \right) - V_{SS} \left(\frac{R1}{R2} \right)$$

$$V_{th(L)} = V_{REF} \left(1 + \frac{R1}{R2} \right) - V_{DD} \left(\frac{R1}{R2} \right)$$

- ❖ Hysteresis = $V_{th(H)} - V_{th(L)}$



Simple Oscillator



- ❖ Combine comparator with hysteresis and RC network = oscillator
- ❖ Voltage at V_+ change instantly with V_{out} :

$$V_H = 2.5 \left(1 + \frac{R1}{R1+R2} \right)$$

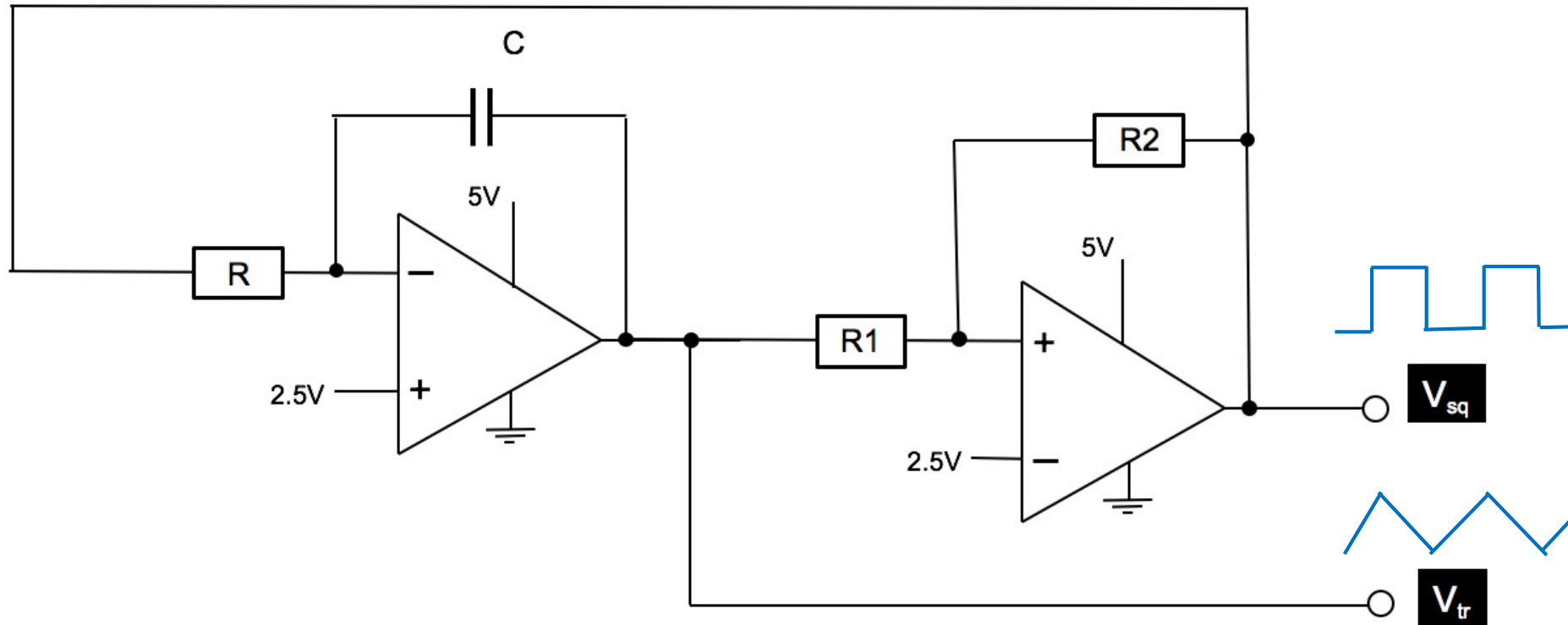
$$V_L = 2.5 \left(\frac{R2}{R1+R2} \right)$$

- ❖ $V_- = V_{th}$ rises and falls exponentially with a time constant of RC between V_H and V_L
- ❖ This is determined by the equation:

$$V_{th} = V_f + (V_i - V_f)e^{-\frac{t}{\tau}}$$

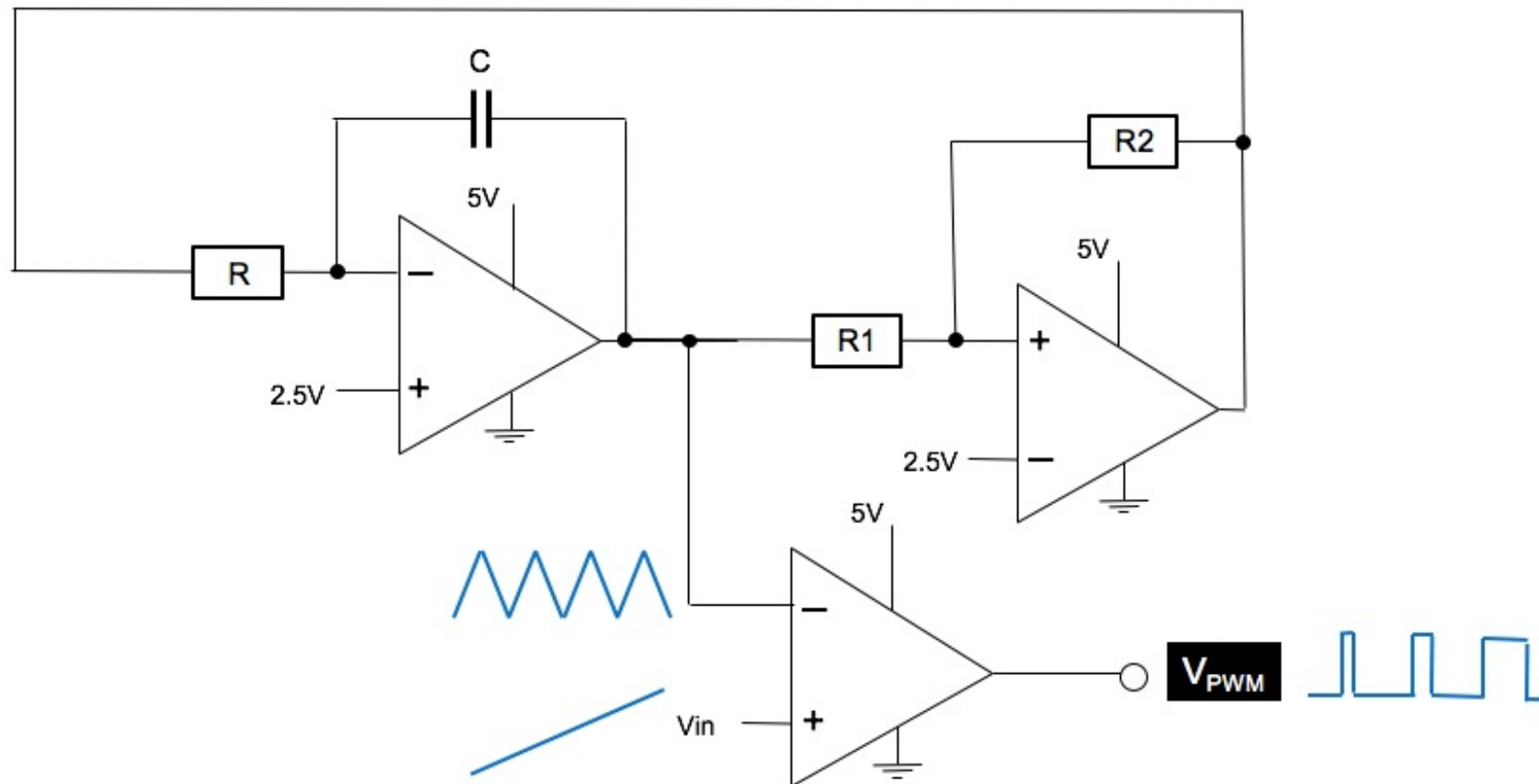
V_i = initial value, V_f = final value, τ = time constant RC

Triangular and Square wave generator



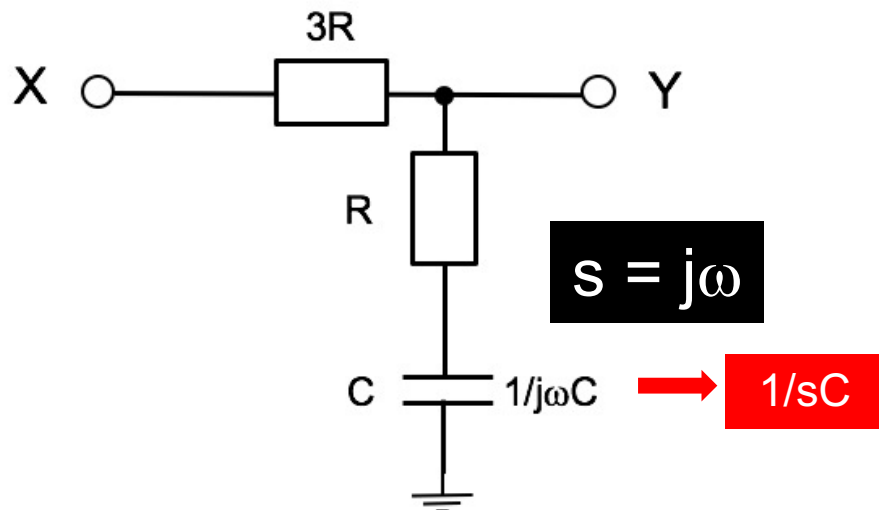
- ❖ Better oscillator circuit using integrator + comparator with hysteresis
- ❖ Integrator output produces a triangular signal
- ❖ Comparator (with hysteresis) produces a square signal
- ❖ Feedback circuit ensures oscillation is maintained

Pulse-width Modulator



- ❖ Comparing triangular signal with V_{in} -> pulse-width modulated output
- ❖ Frequency of triangular signal $\gg V_{in}$ frequency
- ❖ Output pulse width proportional to value of V_{in}
- ❖ Recover V_{in} by lowpass filtering V_{PWM}

Transfer Function of 1st order LP Filter



- ❖ More general if use **complex frequency s** to represent the quantity $j\omega$
- ❖ Covered in Signals and Systems module this term, and Control module next term
- ❖ Express impedance of capacitor as $1/sC$ instead of $1/j\omega C$
- ❖ Capture both steady state (ac) and transient behaviour

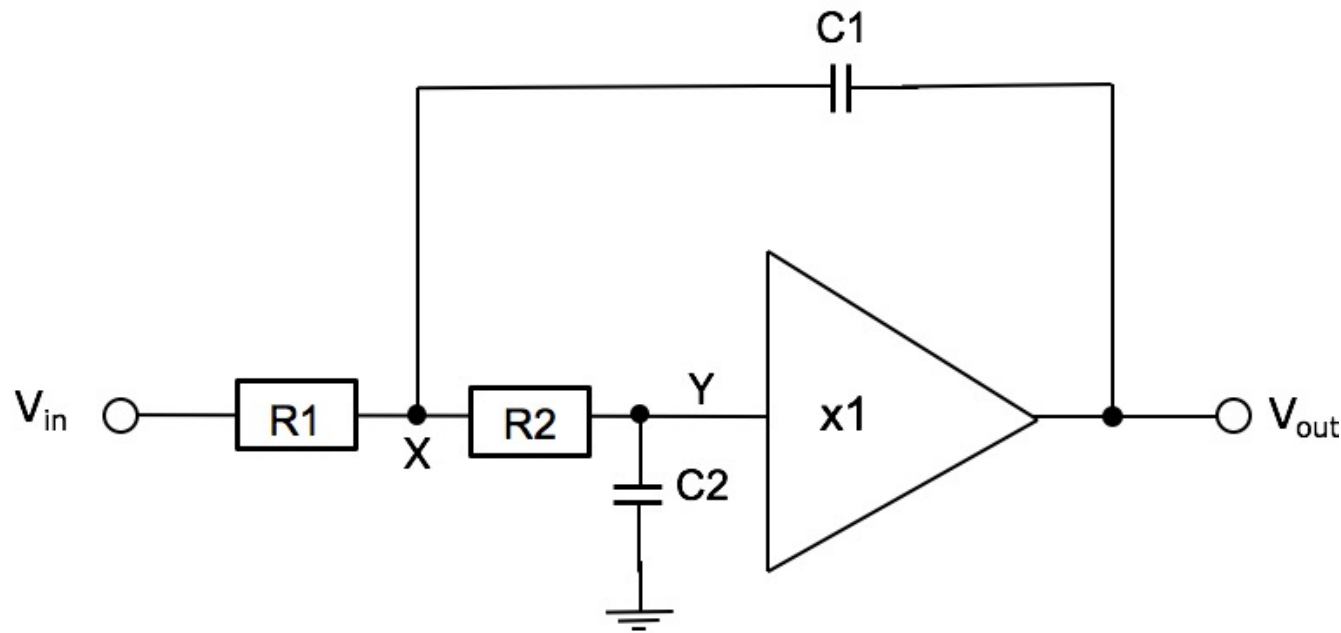
- ❖ Year 1 ADC Part 1 Lecture 11, slide 3

- ❖ Transfer function defined as:
$$H(s) = \frac{Y(s)}{X(s)} = \frac{R+1/sC}{4R+1/sC} = \frac{1+sRC}{1+4sRC}$$

- ❖ Frequency response is calculated as
$$H(s)|_{s=j\omega} = \frac{Y(j\omega)}{X(j\omega)} = \frac{1+j\omega RC}{1+4j\omega RC}$$

- ❖ Easier to perform algebra manipulation than using $j\omega$
- ❖ Provides better intuitions on system behaviour

Sallen-Key 2nd order lowpass filter (1)



- ❖ $Y = V_{out}$ apply KCL at node X, and obtain transfer function in s as:

$$H(s) = \frac{V_{out}(s)}{V_{in}(s)} = \frac{1}{R1C1R2C2} \times \left[\frac{1}{s^2 + s \left(\frac{1}{R2C1} + \frac{1}{R1C1} \right) + \frac{1}{R1C1R2C2}} \right]$$

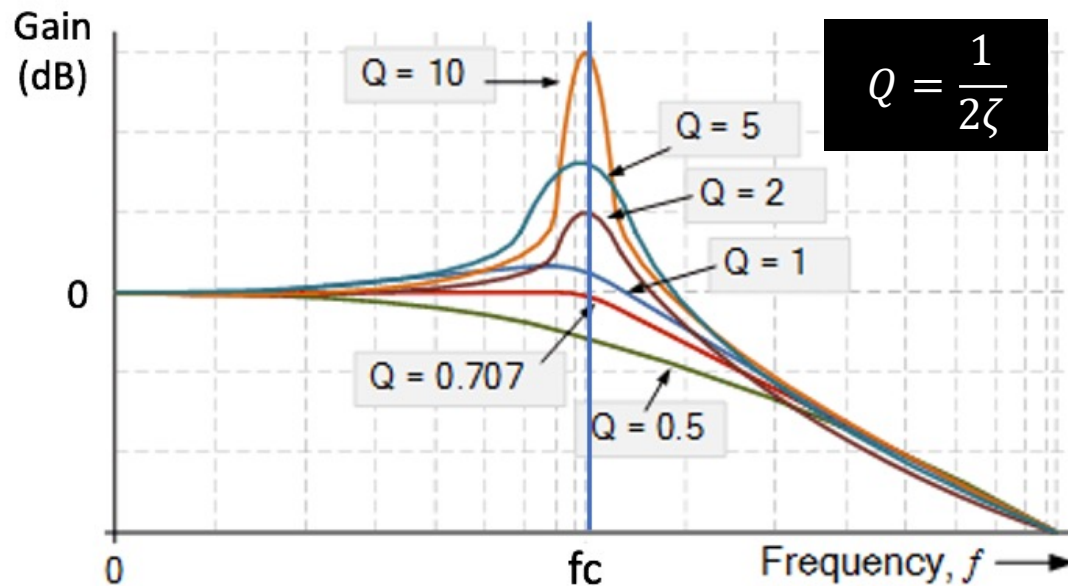
Sallen-Key 2nd order lowpass filter (2)

$$H(s) = \frac{V_{out}(s)}{V_{in}(s)} = \frac{1}{R_1 C_1 R_2 C_2} \times \left[\frac{1}{s^2 + s \left(\frac{1}{R_2 C_1} + \frac{1}{R_1 C_1} \right) + \frac{1}{R_1 C_1 R_2 C_2}} \right]$$

❖ Cut-off frequency f_c is:

$$H(s) = (2\pi f_c)^2 \times \left[\frac{1}{s^2 + 2\zeta(2\pi f_c) s + (2\pi f_c)^2} \right]$$

$$H(s) = G_0 \times \left[\frac{1}{s^2 + a_1 s + a_0} \right]$$



- ❖ a_0 determines the **cut-off frequency** of filter
- ❖ a_1 determines the **resonance behaviour** of filter
- ❖ G_0/a_0 is the **gain of the filter at dc**
- ❖ **Butterworth filter:** $2\zeta = 1.414$, $Q = \frac{1}{2\zeta} = 0.707$
- ❖ **Maximally flat** gain in passband
- ❖ Monotonically decreasing gain in stop band